

AD-A113 974

NAVAL RESEARCH LAB WASHINGTON DC  
INTEGER RESONANCES IN THE MODIFIED BETATRON.(U)  
APR 82 D CHERNIN, P SPRANGLE  
NRL-MR-4691

F/G 20/7

UNCLASSIFIED

NL

1 OF 1  
AD-A  
1-5974



END  
DATE  
FILMED  
105-182  
DTIC

AD A 113974

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER NRL Memorandum Report 4691	2. GOVT ACCESSION NO. 1D-A113974	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle)  INTEGER RESONANCES IN THE MODIFIED BETATRON	5. TYPE OF REPORT & PERIOD COVERED Interim report on continuing problem.	
	6. PERFORMING ORG. REPORT NUMBER	
7. AUTHOR(s)  D. P. Chernin* and P. Sprangle	8. CONTRACT OR GRANT NUMBER(s)	
9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Research Laboratory Washington, D.C. 20375	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS 47-0899-0-2 P.E. 61153N 11 Project RR011-09-41	
11. CONTROLLING OFFICE NAME AND ADDRESS Office of Naval Research Arlington, VA 22209	12. REPORT DATE April 8, 1982	
	13. NUMBER OF PAGES 23	
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)	15. SECURITY CLASS. (of this report) Unclassified	
	15a. DECLASSIFICATION/DOWNGRADING SCHEDULE	
16. DISTRIBUTION STATEMENT (of this Report)  Approved for public release; distribution unlimited.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES  *Berkeley Research Associates, Springfield, VA 22150		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number)  Field errors                      Integer resonances Fourier components            Temperature effect Stationary phase		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number)  The integer resonances affecting beam motion in the presence of external field imperfections in the modified betatron are studied. An upper bound is obtained on the magnitude of field error that may be tolerated. A numerical example shows that for practical parameters the resulting bound is very restrictive. The effect of longitudinal temperature and other possible stabilizing effects are discussed.		

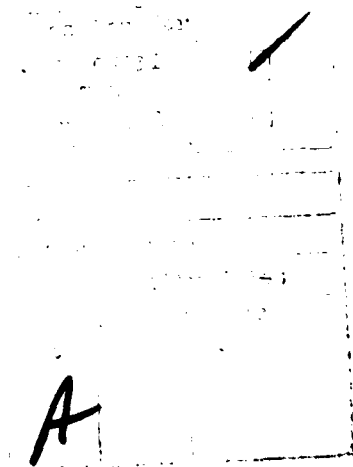
DD FORM 1 JAN 73 1473

EDITION OF 1 NOV 63 IS OBSOLETE  
S/N 0102-014-6601

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

## CONTENTS

I.	INTRODUCTION .....	1
II.	ORBITAL RESONANCES FOR A BEAM .....	1
III.	EFFECT OF FINITE BEAM TEMPERATURE ON RESONANCES .....	6
IV.	CONCLUSIONS .....	8
V.	ACKNOWLEDGMENTS .....	8
	REFERENCES .....	9



# INTEGER RESONANCES IN THE MODIFIED BETATRON

## I. INTRODUCTION

In a conventional betatron, low order resonances between particle motion and field imperfections can be avoided by restricting the beam current so that the tune shift<sup>1</sup> remains sufficiently small. In a modified betatron, the addition of a strong toroidal magnetic field may allow large currents to be accelerated<sup>2,3</sup> but resonances become much more difficult to avoid, especially if one contemplates removing the toroidal field before the beam is extracted. This paper examines the problem of integer resonances in the modified betatron<sup>4</sup> and obtains a condition bounding the rate of change of the fields: when the condition is satisfied the resonances are passed through with sufficient speed so that the beam is not significantly disturbed. We consider here only errors in the fields themselves, not in field gradients, so we discuss only the integer, not the half integer resonances.

In what follows we will first consider a "cold" beam, that is, one in which there is no spread in longitudinal energy or, therefore, in circulation frequency about the machine. The effect of orbital resonances on such a cold beam will be seen to place rather severe limits on the magnitude of the tolerable field imperfections. When the effects of temperature are taken into account however a numerical example below will illustrate a reduction of the effect of the resonance on the motion of the beam center of mass. An explanation of this temperature effect will be given.

## II. ORBITAL RESONANCES FOR A COLD BEAM

We consider a beam of circular cross section and uniform density and current profiles as shown in Fig. 1. The torus has a major radius  $r_0$  and minor radius  $a$ ; the chamber is assumed to be perfectly

conducting as far as the rapidly varying part of the self fields is concerned. The beam radius is  $r_b$  with center located at  $r = r_0 + \Delta r$ ,  $z = \Delta z$  as shown in the figure. If we define the displacement of a particle from the design orbit  $r = r_0$ ,  $z = 0$  as  $r_1 = \Delta r + \delta r$ ,  $z_1 = \Delta z + \delta z$  then the equations of motion for  $r_1$  and  $z_1$  are, to first order in the displacement from the design orbit:

$$\ddot{r}_1 + \frac{\dot{\gamma}_0}{\gamma_0} \dot{r}_1 + \Omega_{z0}^2 (1 - n - n_s) r_1 = \frac{e \dot{B}_{\theta 0}}{2 m \gamma_0 c} z_1 + \Omega_{\theta 0} \dot{z}_1 - \frac{\omega_b^2}{2 \gamma_0^2} \left( 1 - \frac{r_b^2}{a^2} \right) \Delta r - \frac{e}{m \gamma_0} \left[ \tilde{E}_r + \beta_0 \tilde{B}_z + \Omega_{z0} \int_0^t dt' \tilde{E}_\theta(t') \right] \quad (1a)$$

$$\ddot{z}_1 + \frac{\dot{\gamma}_0}{\gamma_0} \dot{z}_1 + \Omega_{z0}^2 (n - n_s) z_1 = - \frac{e \dot{B}_{\theta 0}}{2 m \gamma_0 c} r_1 - \Omega_{\theta 0} \dot{r}_1 - \frac{\omega_b^2}{2 \gamma_0^2} \left( 1 - \frac{r_b^2}{a^2} \right) \Delta z - \frac{e}{m \gamma_0} [\tilde{E}_z - \beta_0 \tilde{B}_r] \quad (1b)$$

where

$\gamma_0$  = energy of particle on "ideal" design orbit (in units of  $mc^2$ )

$\Omega_{z0} = e B_{z0} / m \gamma_0 c$

$\Omega_{\theta 0} = e B_{\theta 0} / m \gamma_0 c$

$B_{z0}$  = vertical magnetic field at design orbit

$B_{\theta 0}$  = toroidal magnetic field

$n$  = betatron field index (assumed constant here)

$n_s$  = self field index =  $\omega_b^2 / (2 \gamma_0^2 \Omega_{z0}^2)$

$\omega_b$  = beam plasma frequency =  $(4 \pi n_0 e^2 / m \gamma_0)^{1/2}$

$e$ ,  $m$  = magnitude of electron charge, rest mass

and where field components with a "wiggle" on the right hand sides of (1a, b) denote the value of the field imperfection which in general will depend on the value of  $\theta$ , the azimuthal position of the particle. When deriving (1a, b) we have allowed all fields to depend on time; we have therefore included the inductive poloidal electric field ( $\dot{B}_{\theta 0}$  terms). Also included are the effect of wall image charges and currents ( $r_b^2/a^2$  terms), present when the beam is displaced from the center of the chamber.

We desire to have equations which describe only the motion of the beam center,  $\Delta r(\theta, t)$ ,  $\Delta z(\theta, t)$ . To this end we define a distribution function  $f$  as

$$f(r, \theta, z, v_r, v_\theta, v_z, t) \equiv \sum_{\mathbf{r}^{(0)}, \mathbf{v}^{(0)}} g(\mathbf{r}^{(0)}, \mathbf{v}^{(0)}) \delta(r - \hat{r}) \frac{\delta(\theta - \hat{\theta})}{r} \delta(z - \hat{z}) \delta^{(3)}(\mathbf{v} - \hat{\mathbf{v}}) \quad (2)$$

where  $\mathbf{r}^{(0)}$  and  $\mathbf{v}^{(0)}$  are particle initial conditions,  $\hat{r}$ ,  $\hat{\theta}$ ,  $\hat{z}$ , and  $\hat{\mathbf{v}}$  are the solutions for the particle trajectories as functions of initial position, velocity, and time, and where  $g(\mathbf{r}^{(0)}, \mathbf{v}^{(0)})$  is a weighting function.

**We then have that**

$$\Delta r(\theta, t) = \frac{\int r dr dz dv (r - r_0) f}{\int r dr dz dv f} = \frac{\Sigma g(\mathbf{r}^{(0)}, \mathbf{v}^{(0)}) (\hat{r} - r_0) \delta(\theta - \hat{\theta})}{\Sigma g(\mathbf{r}^{(0)}, \mathbf{v}^{(0)}) \delta(\theta - \hat{\theta})} \equiv \langle r_1 \rangle. \quad (3)$$

A similar expression holds for  $\Delta z(\theta, t)$ . It may be similarly shown that, for a cold beam,

$$\langle \dot{r}_1 \rangle = \left( \frac{\partial}{\partial t} + \Omega_{z0} \frac{\partial}{\partial \theta} \right) \Delta r \quad (4)$$

$$\langle \ddot{r}_1 \rangle = - \left( \frac{\partial}{\partial t} + \Omega_0 \frac{\partial}{\partial \theta} \right)^2 \Delta r \quad (5)$$

where, of course, analogous expressions hold for  $\langle z_1 \rangle$ ,  $\langle \dot{z}_1 \rangle$  and  $\langle \ddot{z}_1 \rangle$ . In Eqs. (4) and (5) we have assumed that all particles circulate the machine with  $\dot{\theta} = \Omega_{z0}$ . This assumption will be relaxed in the next section where the effects of finite longitudinal temperature are considered.

Using this averaging procedure on (1a, b) one obtains equations for the beam center motion. Though these may be solved in general, the special choice  $n = 1/2$  (which is consistent with our assumption of a circular beam) simplifies the analysis

With  $n = 1/2$  and defining

$$\Delta\psi = \Delta r + \Delta z \equiv \sum_{j=1}^{\infty} \overline{\Delta\psi_j} e^{i\psi_j} \quad (6)$$

the equation for  $\overline{S_{ij}}$  is

$$\begin{aligned} \frac{\partial^2}{\partial t^2} \overline{\Delta \psi_i} + \left[ \frac{\dot{\gamma}_0}{\gamma_0} + i\Omega_{z0} + 2i\Omega_{z0} \right] \frac{\partial \overline{\Delta \psi_i}}{\partial t} \\ + \left[ \Omega_{z0} \left( \frac{1}{2} - \frac{r_i^2}{a^2} n_i - l^2 \right) + i\Omega_{z0} \frac{\dot{\gamma}_0}{\gamma_0} + i \frac{e \dot{B}_{z0}}{2m\gamma_0} \right. \\ \left. + \Omega_{z0} + i\Omega_{z0} \right] \overline{\Delta \psi_i} \\ = F_i \end{aligned} \quad (7)$$

where  $F_l$  is the  $l$ -th Fourier component of

$$- \frac{e}{m\gamma_0} \left[ \tilde{E}_r + \beta_0 \tilde{B}_z + i(\tilde{E}_z - \beta_0 \tilde{B}_r) + \Omega_{z0} \left\langle \int_0^t dt' \tilde{E}_\theta(t') \right\rangle \right].$$

Equation (7) may be solved, assuming the functions multiplying derivatives of  $\overline{\Delta\psi}_l$  are slowly varying over the period of a betatron oscillation:

$$\overline{\Delta\psi}_l \approx (\gamma_0 \omega_0)^{-1/2} \int_0^t dt' e^{-i \int_{t'}^t dt'' \left[ \frac{1}{2} \Omega_{z0} + l \Omega_{z0} \right]} \left[ \frac{\gamma_0(t')}{\omega_0(t')} \right]^{1/2} \sin \left[ \int_{t'}^t dt'' \omega_0 \right] F_l(t') \quad (8)$$

where

$$\omega_0(t) \equiv \left[ \Omega_{z0}^2 \left( \frac{1}{2} - \frac{r_b^2}{a^2} n_s \right) + \frac{1}{4} \Omega_{z0}^2 \right]^{1/2}. \quad (9)$$

For long times (many betatron periods) the integral in (8) may be evaluated by the method of stationary phase. The points of stationary phase (resonance points) occur when

$$\Omega_l^\pm \equiv -\frac{1}{2} \Omega_{z0} - l \Omega_{z0} \pm \omega_0 = 0 \quad (10)$$

for a given  $l$ . This is just the condition that the betatron frequency be  $l$  times the fundamental cyclotron frequency,  $\Omega_{z0}$ . Condition (10) may also be written

$$B_{z0} = -\frac{1}{l} \left( l^2 + \frac{r_b^2}{a^2} n_s - \frac{1}{2} \right) B_{z0}. \quad (11)$$

For positive  $B_{z0}$  and  $B_{z0}$  (11) may be satisfied only by negative  $l$  and for such  $l$  (10) may be satisfied only for the lower sign (fast mode resonance). Evaluating (8) then gives

$$\overline{\Delta\psi}_l \sim i \left( \frac{\pi}{2} \right)^{1/2} \left[ \frac{\gamma_0(t_-)}{\gamma_0(t) \omega_0(t) \omega_0(t_-)} \right]^{1/2} \frac{F_l(t_-)}{|\dot{\Omega}_l^-(t_-)|^{1/2}} e^{i \int_{t_-}^t \Omega_l^- dt'' \pm \pi/4} \quad (12)$$

where  $t_-$  is the time at which  $\Omega_l^- = 0$  and where the  $+$  or  $-$  sign is used in the exponent according as  $\dot{\Omega}_l^-(t_-) > 0$  or  $< 0$  respectively.

If we neglect the possibility of cancellation due to different phases as we pass through different resonances and if we interpret  $F_l$  generically as  $\left[ -\frac{e}{m\gamma_0} \delta f_l \right]$  where  $\delta f_l$  is the  $l$ -th Fourier component of any field error, we may obtain a lower bound on  $|\dot{\Omega}_l^-|$  by requiring



$$|\overline{\Delta\psi}_l| \ll a \quad (13)$$

which gives

$$|\dot{\Omega}_l^-| \gg \frac{\pi}{2} \left[ \frac{e\delta f_l}{m\gamma_0\omega_0 a} \right]^2 \quad (14)$$

which is our basic result. For  $\gamma_0$  large enough that we may neglect  $\dot{\Omega}_{z0}$  compared to  $\dot{\Omega}_{u0}$  and  $r_b^2 n_s / a^2$  compared to  $1/2$ , this constraint may be rewritten, using the relations

$$\dot{\Omega}_l^- = - \frac{l^2}{l^2 + 1/2} \dot{\Omega}_{u0} \quad (15)$$

and

$$\omega_0 = \frac{l^2 + 1/2}{2|l|} \Omega_{z0} \quad (16)$$

as

$$|\dot{\Omega}_{u0}| \gg \frac{2\pi}{l^2 + 1/2} \left[ \frac{\delta f_l}{B_{z0}} \frac{c}{a} \right]^2 \quad (17)$$

As an example we consider the problem of passing through the  $l = -1$  resonance. We consider a hypothetical experiment ( $r_0 = 1$  m,  $a = 10$  cm,  $r_b = 1$  cm) in which  $\gamma_0$  is increased linearly in time from an initial (injection) value of 7 to a final value ( $t_{\text{final}} = 1$  millisecond) of 100 while simultaneously  $B_{u0}$  is decreased from 1.5 kg to 0. The  $l = -1$  resonance will occur at  $t = 627 \mu\text{s}$  at which time  $B_{z0} = 1120$  g,  $B_{u0} = 560$  g, and  $\gamma_0 = 65.3$ . At resonance,  $\dot{\Omega}_{u0} = -6.2 \times 10^{11} \text{ sec}^{-2}$ . Substituting in the expression (17) we obtain an upper bound on the allowable field error

$$\frac{\delta f_{-1}}{B_{z0}} \ll 1.3 \times 10^{-4},$$

a rather severe requirement.

We conclude that, at least for the case of a cold beam, it may not be desirable to remove the toroidal field and pass through these resonances. Perhaps the toroidal field may be reduced somewhat from its initial value, assuming the high  $l$  resonances are not too important and can be easily passed through. It may then be possible, by the use of an intentionally introduced field perturbation to use a low  $l$  resonance in a controlled way to extract the beam before  $B_u$  is completely removed.

It should be noted that it is possible, at least in principle, to avoid the integer resonances altogether by raising both  $B_{z0}$  and  $B_{\theta 0}$  proportionately and in such a way that condition (11) is never satisfied for any  $l$ . At the end of such an acceleration cycle however one will have a very large toroidal magnetic field in the device, possibly complicating the extraction process.

The above results apply to a beam all of whose particles are traveling to lowest order at the same azimuthal angular velocity. All particles are then in resonance at precisely the same moment and receive the same periodic perturbations to their orbits. In the next section we relax this assumption and examine the behavior of a beam, the particles of which possess a spread in energy.

### III. EFFECT OF FINITE BEAM TEMPERATURE ON RESONANCES

To calculate the effect of beam temperature on beam behavior near a resonance we consider an ensemble of beams, each cold and each consisting of particles traveling with a zero order angular frequency  $\dot{\theta}_0$  given by

$$\dot{\theta}_0 = \Omega_{z0} - kP \quad (18)$$

where  $P$  is the canonical angular momentum of a particle which is related to the difference in energy between the particle under consideration and the (reference) particle maintained at the design orbit  $r = r_0, z = 0$  by

$$P = \frac{\Delta\gamma mc^2}{\Omega_{z0}}, \quad (19)$$

and where, in (18),

$$-k \equiv \left( \frac{1}{\gamma_0^2} - \frac{1}{1/2 - n_r} \right) / \gamma_0 m r_0^2. \quad (20)$$

For each cold beam, relations (4) and (5) are then modified by the replacement

$$\Omega_{z0} \rightarrow \Omega_{z0} - kP \quad (21)$$

and therefore we may obtain the solution for each cold beam by making the replacement, in Eq. (8),

$$l\Omega_{z0} \rightarrow l(\Omega_{z0} - kP). \quad (22)$$

The behavior of the actual warm beam will then be given by

$$\overline{\Delta\psi}_1 \approx \left\langle (\gamma_0 \omega_0)^{-1/2} \int' dt' e^{-i \int' dt'' \left[ \frac{1}{2} \Omega_{+0} + i(\Omega_{+0} - kP) \right]} \left[ \frac{\gamma_0(t')}{\omega_0(t')} \right]^{1/2} \sin \left[ \int' dt'' \omega_0 \right] F_1(t') \right\rangle_P \quad (23)$$

where the average is defined over some normalized distribution function in  $P$ , i.e.

$$\langle \dots \rangle_P = \int_{-\infty}^{\infty} dPG(P) \dots \quad (24)$$

In Eq. (23) we can immediately anticipate the effect of temperature on the behavior of the beam: the entire effect is included in the phase factor, in the term  $kP$ . Such a term when averaged over any reasonable momentum distribution will give a reduction in amplitude of the average as the "width" of  $G(P)$  is increased. Physically this means that the various particles of different energies within the beam receive, when passing through resonance, displacements in *slightly different directions*. The net effect on the motion of the beam center is therefore reduced. (Though our linearized treatment here necessarily includes a fixed beam size, it may in fact be the case that a warm beam will just expand slightly while passing through resonance while the motion of the beam center remains relatively undisturbed.)

As an example we consider a beam made up of particles having the energy distribution

$$G_E(\Delta\gamma) = \begin{cases} 1/T_L & |\Delta\gamma| < T_L/2 \\ 0 & |\Delta\gamma| > T_L/2 \end{cases} \quad (25)$$

where  $T_L$  is a measure of the longitudinal temperature and where  $\Delta\gamma$  is related to  $P$  by Eq. (19). We consider again the hypothetical experiment described in the preceding section. For  $\delta f_{-1}/B_{+0} = 5 \times 10^{-3}$  the results of a numerical evaluation of Eq. (23) are shown in Figs. 2-5 which correspond to  $T_L = (0., 0.5, 1.0, 2.0)$ . In each figure the real part of  $\overline{\Delta\psi}_1$  is plotted, in centimeters, versus time, in seconds. The resonance condition, Eq. (11), is satisfied at the center of the time axis. Total elapsed time is 2.1  $\mu$ s. The chamber diameter,  $2a = 20$  cm is indicated by solid horizontal lines on each plot. We observe that for this example,  $T_L = 1.0$ , or a 0.5 MeV energy spread, is adequate to smooth out the effect of the resonance. This is the same order of magnitude of spread needed to damp the negative mass/kink instability in this device<sup>5</sup>.

#### IV. CONCLUSIONS

We have obtained a bound on the magnitude of field errors that can be tolerated in a modified betatron in order that certain integer resonances may be safely passed through. We have found that for practical parameters the bound is extremely restrictive. The basic difficulty stems from the fact that unless the external parameters of the system are changed very quickly the orbits remain in or near resonance for many betatron oscillations, allowing the displacements to grow to large levels. Such a result suggests that nonlinear effects may play an important role in beam behavior near a resonance. For example, one may ask whether the radial dependence of  $B_z$  would be sufficient to "detune" the resonance as the beam moves a finite but small distance from its equilibrium position. This possibility is receiving further study.

We have also shown that a finite longitudinal beam temperature acts to reduce the effect of the resonance on the motion of the center of the beam. The temperature spread required appears to be comparable, in a specific example, to that needed to stabilize certain micro instabilities. However, it remains unresolved in this analysis whether the beam expands when passing through a resonance. Such behavior, of course, if severe, could be as unacceptable as large, whole beam displacement.

Should it be possible to achieve significantly lower field errors than those used in our example (0.5%) or if it is possible experimentally to detect and correct by some feedback mechanism the sudden, resonant displacement of the beam then perhaps lower toroidal fields may be employed initially and be removed either during or following acceleration. The effects of passage through the low  $l$  resonances may thereby be reduced to a tolerably small level.

#### V. ACKNOWLEDGMENTS

This work was supported by the Office of Naval Research.

REFERENCES

1. L.J. Laslett in "Proc. of the 1963 Summer Study on Storage Rings, Accelerators and Experimentation at Super-High Energies" BNL-7534.
2. P. Sprangle and C.A. Kapetanakis, J. Appl. Phys. **49**, 1 (1978).
3. N. Rostoker, Bull. APS. **25**, 854 (1980).
4. Laslett (ERAN-51, Jan 1970 (unpublished)) has discussed certain aspects of the resonance problem in the ERA with a toroidal field. He has derived explicit expressions for  $\nu$ .
5. P. Sprangle and J.L. Vomvoridis, NRL Memorandum Report 4688 (to be published).

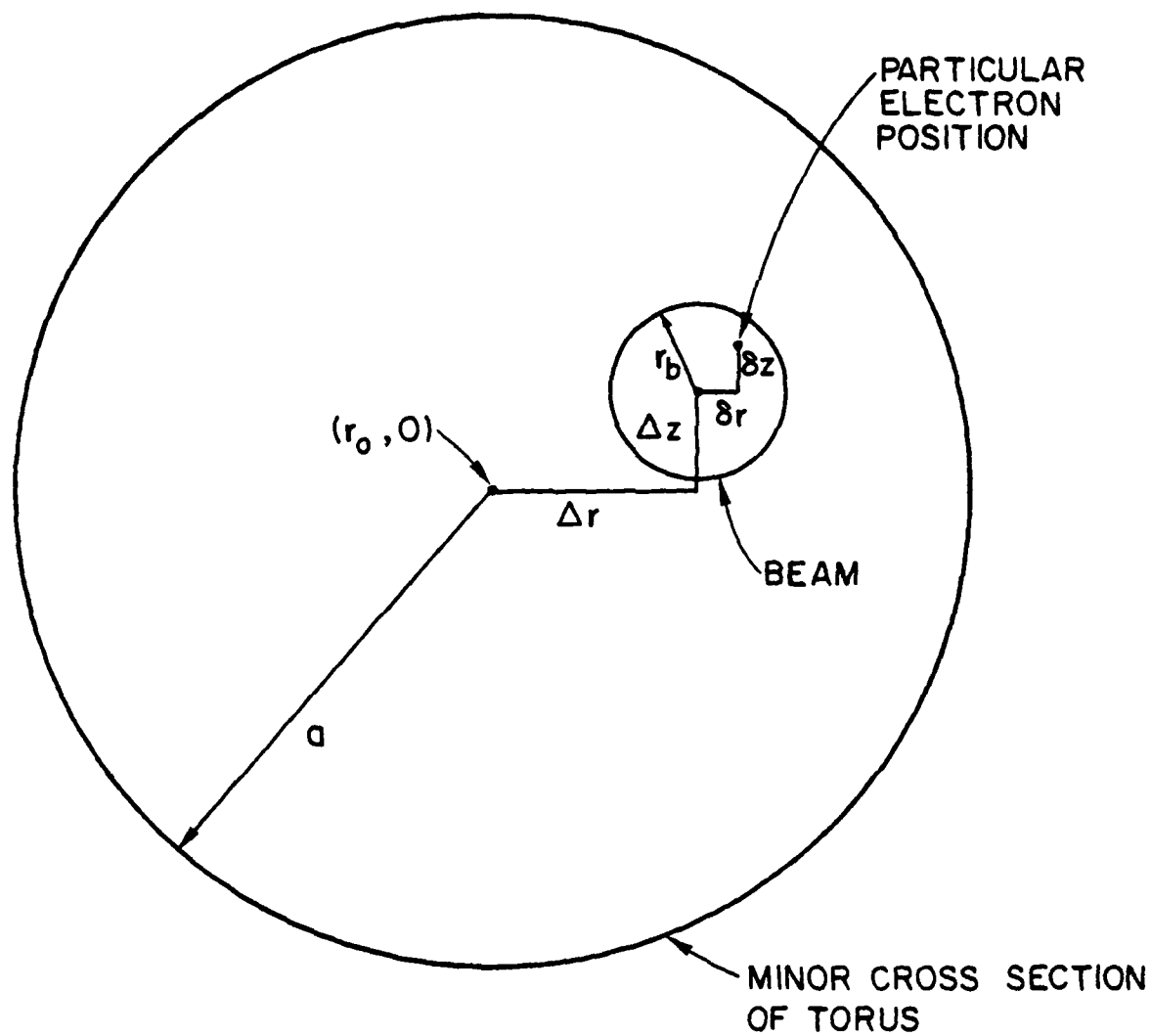


Fig. 1 — Minor cross section of modified betatron showing beam center and particle coordinates.  
The major radius of the device is  $r_0$ .

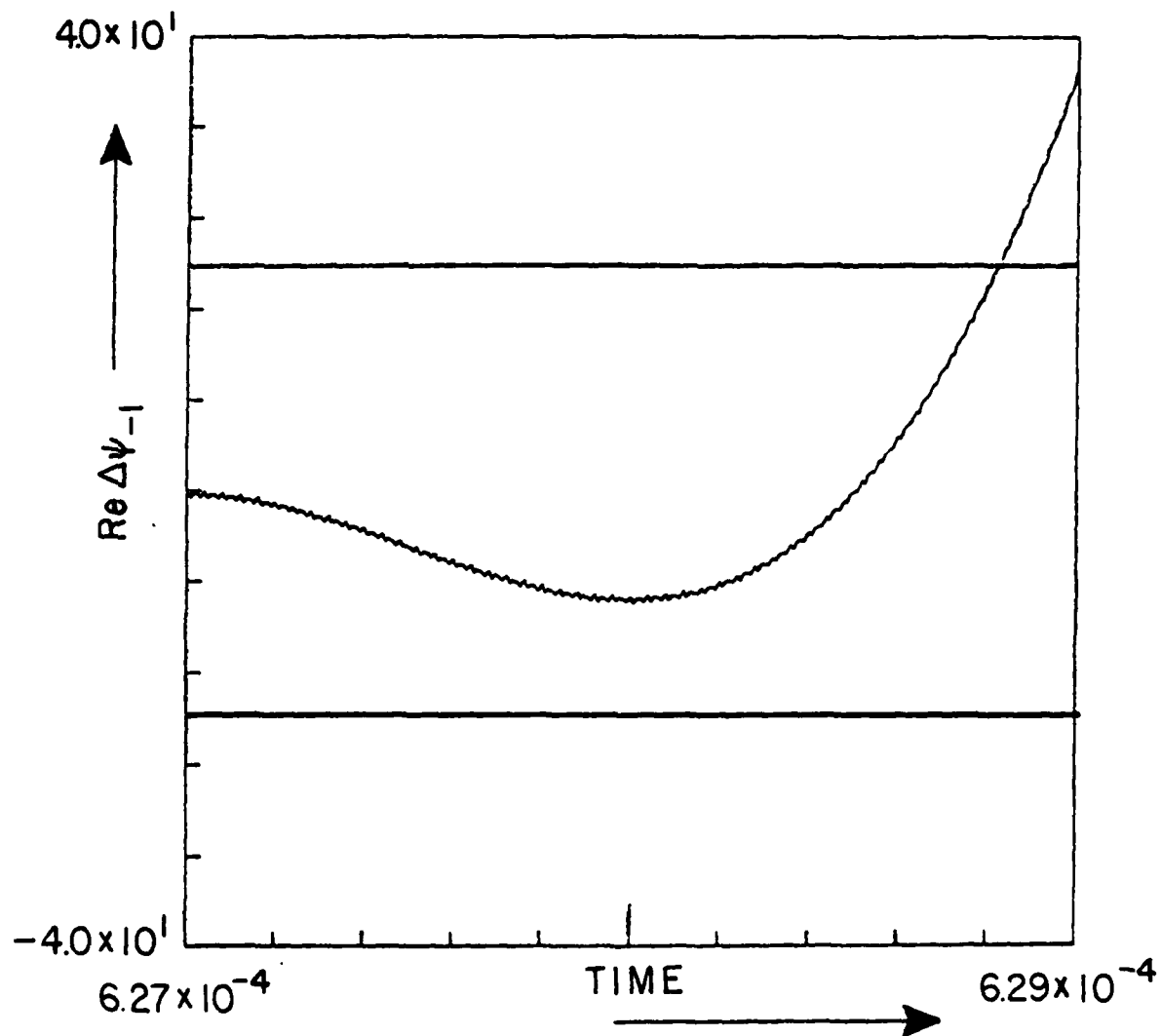


Fig. 2 —  $\text{Re } (\Delta\psi_{-1})$  vs. time for  $T_L \approx 0$ .

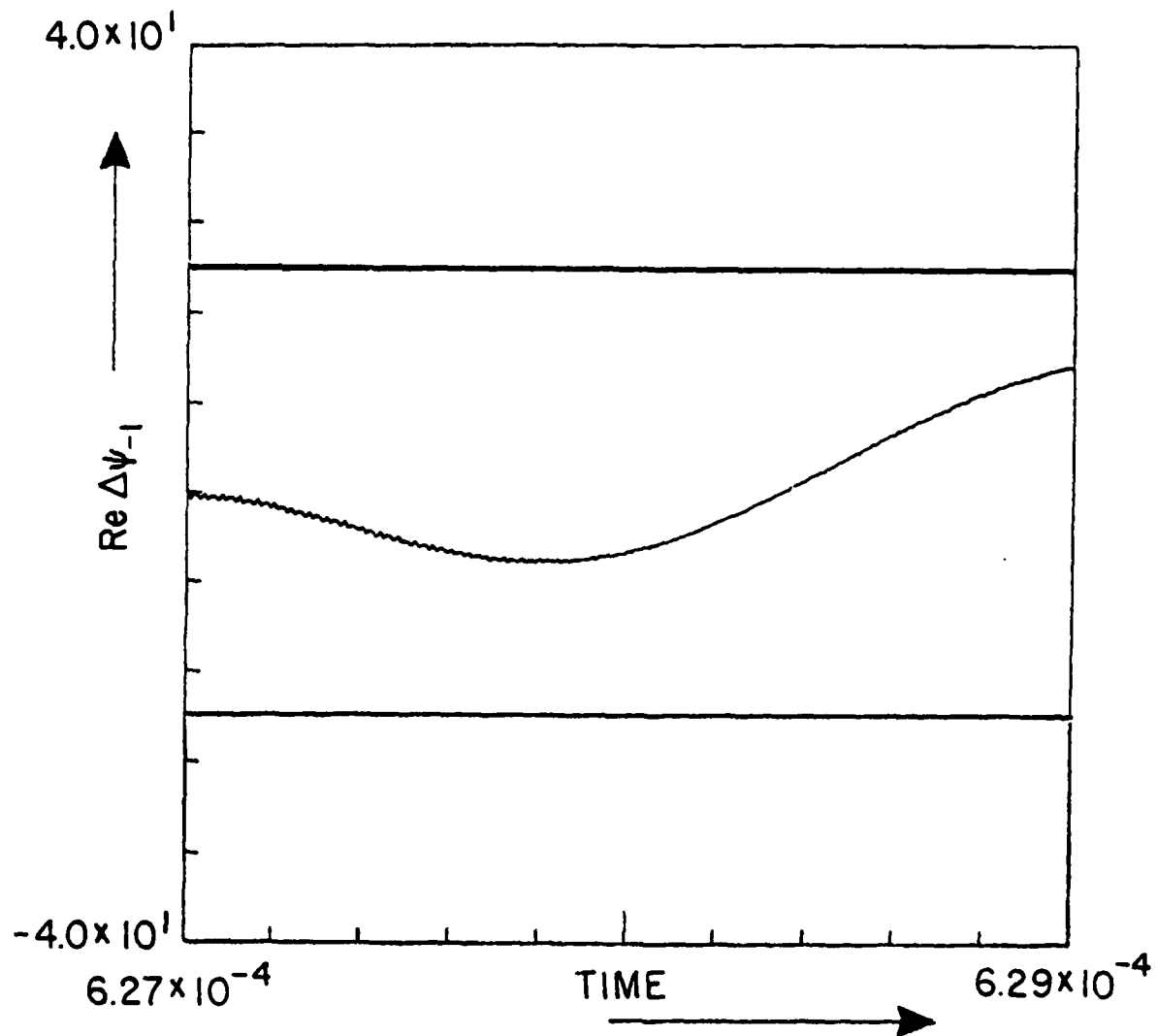


Fig. 3 -  $\text{Re } (\Delta\psi_{-1})$  vs. time for  $T_L = 0.5$ .



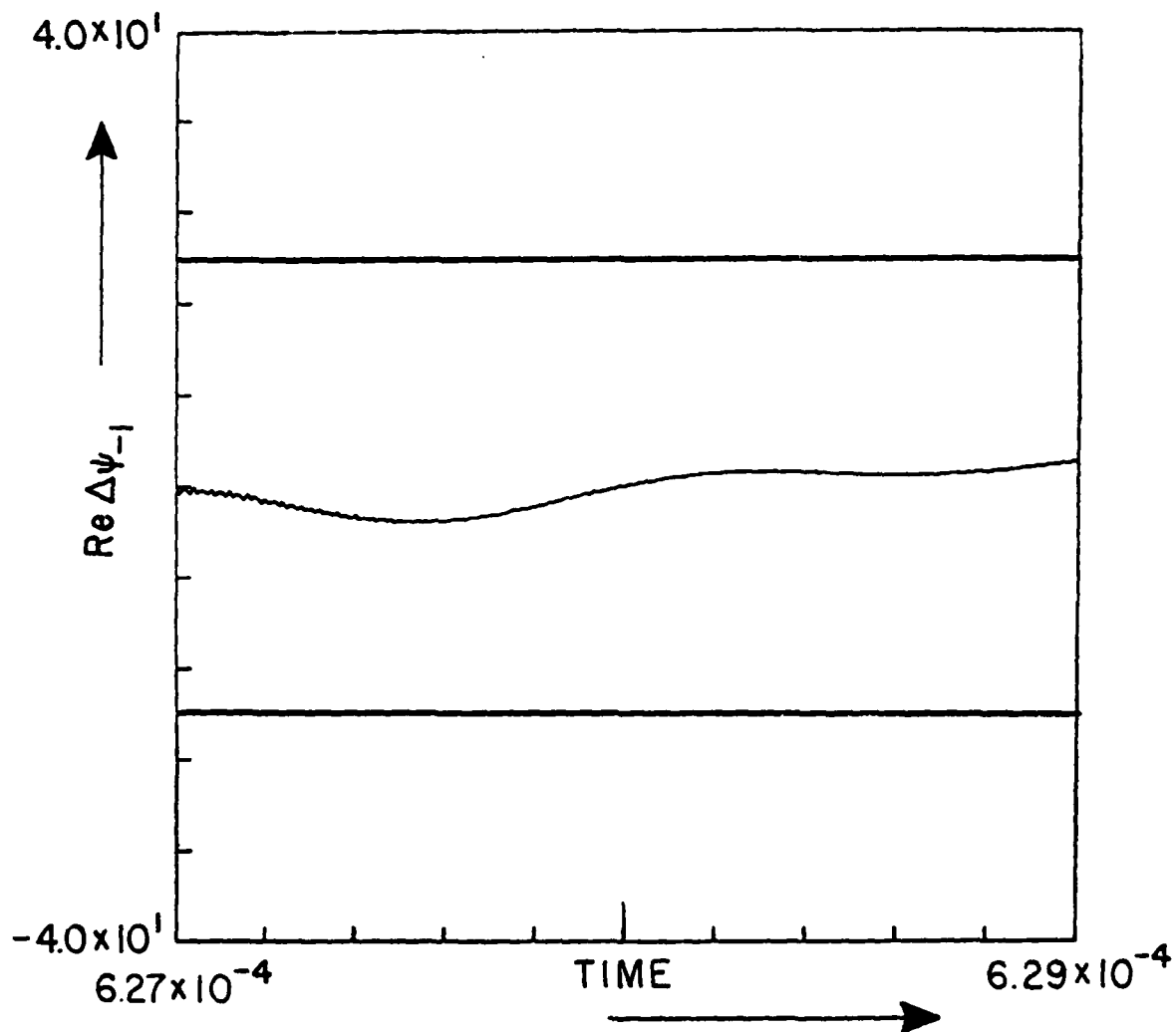


Fig. 4 -  $\text{Re } (\Delta\psi_{-1})$  vs. time for  $T_L = 1.0$ .

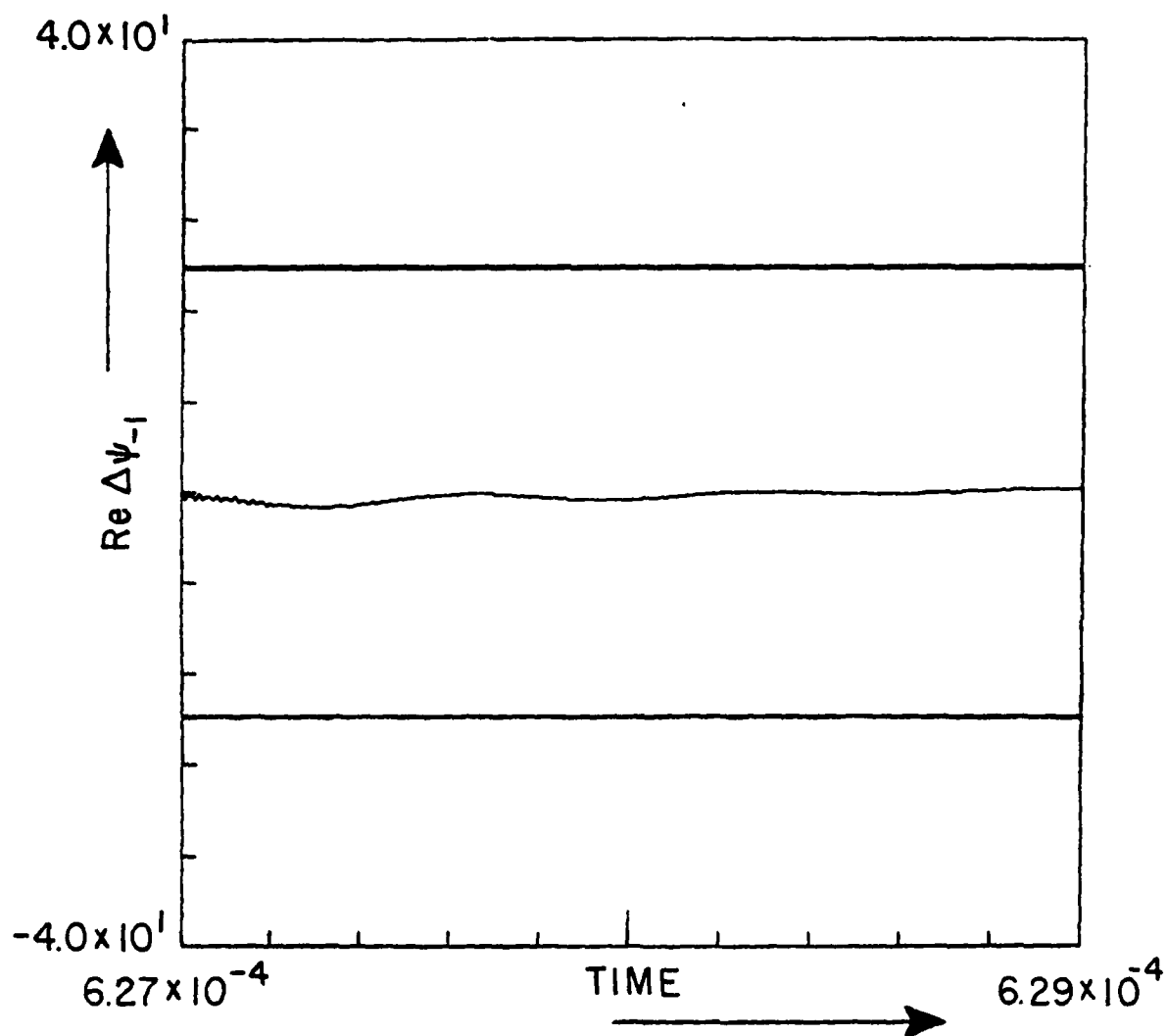


Fig. 5 —  $\text{Re } (\Delta\psi_{-1})$  vs. time for  $T_L = 2.0$ .

DISTRIBUTION LIST\*

Naval Research Laboratory  
4555 Overlook Avenue, S.W.  
Washington, D.C. 20375

Attn: Code 1000 - CAPT. E. E. Henifin  
1001 - Dr. A. Berman  
4700 - Dr. S. Ossakow (26 copies)  
4701 - Mr. J. Brown  
4740 - Dr. V. L. Granatstein (20 copies)  
4740 - Dr. K. R. Chu  
4740 - Dr. C. W. Roberson  
4790 - Dr. P. Sprangle (100 copies)  
4790 - Dr. C. M. Tang  
4790 - Dr. M. Lampe  
4790 - Dr. W. M. Manheimer  
6603S- Dr. W. W. Zachary  
6650 - Dr. L. Cohen  
6656 - Dr. N. Seeman  
6850 - Dr. L. R. Whicker  
6805 - Dr. S. Y. Ahn  
6805 - Dr. R. K. Parker (20 copies)  
6875 - Dr. R. Wagner

On Site Contractors:

Code 4740 - Dr. L. Barnett (B-K Dynamics)  
4740 - Dr. D. Dialetis (SAI)  
4740 - Dr. Y. Y. Lau (SAI)  
4790 - Dr. A. T. Drobot (SAI)  
4790 - Dr. J. Vomvoridis (JAYCOR)  
4790 - Dr. H. Freund (SAI)

\* Every name listed on distribution gets one copy except for those where extra copies are noted.

Dr. Tony Armstrong  
SAI, Inc.  
P. O. Box 2351  
La Jolla, CA 92038

Dr. Robert Behringer  
ONR  
1030 E. Green  
Pasadena, CA 91106

Dr. G. Bekefi (5 copies)  
Massachusetts Institute of Technology  
Bldg. 26  
Cambridge, MA 02139

Dr. Arden Bement (2 copies)  
Deputy Under Secretary of Defense  
for R&AT  
Room 3E114, The Pentagon  
Washington, D.C. 20301

Lt Col Rettig P. Benedict Jr., USAF  
DARPA/STO  
1400 Wilson Boulevard  
Arlington, VA 22209

Dr. T. Berlincourt  
Code 420  
Office of Naval Research  
Arlington, VA 22217

Dr. I. B. Bernstein (2 copies)  
Yale University  
Mason Laboratory  
400 Temple Street  
New Haven, CT 06520

Dr. Charles Brau (2 copies)  
Applied Photochemistry Division  
Los Alamos National Scientific  
Laboratory  
P. O. Box 1663, M.S. - 817  
Los Alamos, NM 87545

Dr. R. Briggs (L-71)  
Lawrence Livermore National Lab.  
P. O. Box 808  
Livermore, CA 94550

Dr. Fred Burskirk  
Physics Department  
Naval Postgraduate School  
Monterey, CA 93940

Dr. K. J. Button  
Massachusetts Institute of Technology  
Francis Bitter National Magnet Lab.  
Cambridge, MA 02139

Dr. Gregory Canavan  
Director, Office of Inertial Fusion  
U. S. Department of Energy  
M.S. C404  
Washington, D.C. 20545

Prof. C. D. Cantrell  
Center for Quantum Electronics  
& Applications  
The University of Texas at Dallas  
P. O. Box 688  
Richardson, TX 75080

Dr. Maria Caponi  
TRW, Building R-1, Room 1070  
One Space Park  
Redondo Beach, CA 90278

Dr. J. Cary  
Los Alamos National Scientific  
Laboratory  
MS 608  
Los Alamos, NM 87545

Dr. Weng Chow  
Optical Sciences Center  
University of Arizona  
Tucson, AZ 85721

Dr. Peter Clark  
TRW, Building R-1, Room 1096  
One Space Park  
Redondo Beach, CA 90278

Dr. Robert Clark  
P. O. Box 1925  
Washington, D.C. 20013

Dr. William Colson  
Quantum Institute  
Univ. of California at Santa Barbara  
Santa Barbara, CA 93106

Dr. William Condell  
Code 421  
Office of Naval Research  
Arlington, VA 22217

Dr. Richard Cooper  
Los Alamos National Scientific  
Laboratory  
P. O. Box 1663  
Los Alamos, NM 87545

Cmdr. Robert Cronin  
NFOIO Detachment, Suitland  
4301 Suitland Road  
Washington, D.C. 20390

Dr. R. Davidson (5 copies)  
Plasma Fusion Center  
Massachusetts Institute of  
Technology  
Cambridge, MA 02139

Dr. John Dawson (2 copies)  
Physics Department  
University of California  
Los Angeles, CA 90024

Dr. David Deacon  
Physics Department  
Stanford University  
Stanford, CA 94305

Defense Technical Information  
Center (12 copies)  
Cameron Station  
5010 Duke Street  
Alexandria, VA 22313

Dr. Francesco De Martini  
Istituto de Fiscia  
G. Marconi" Univ.  
Piazzo delle Science, 5  
ROMA00185 ITALY

Prof. P. Diamant  
Columbia University  
Dept. of Electrical Engineering  
New York, NY 10027

Prof. J. J. Doucet (5 copies)  
Ecole Polytechnique  
91128 Palaiseau  
Paris, France

Dr. John Elgin (2 copies)  
Imperial College  
Dept. of Physics (Optics)  
London SWF, England

Dr. Luis R. Elias (2 copies)  
Quantum Institute  
University of California  
Santa Barbara, CA 93106

Dr. David D. Elliott  
SRI International  
33 Ravenswood Avenue  
Menlo Park, CA 94025

Dr. Jim Elliot (2 copies)  
X-Division, M.S. 531  
Los Alamos National Scientific  
Laboratory  
Los Alamos, NM 87545

Director (2 copies)  
National Security Agency  
Fort Meade, MD 20755  
ATTN: Mr. Richard Foss, A42

Dr. Robert Fossum, Director  
(2 copies)  
DARPA  
1400 Wilson Boulevard  
Arlington, VA 22209

Dr. Edward A. Frieman  
Director, Office of Energy Research  
U. S. Department of Energy  
M.S. 6E084  
Washington, D.C. 20585

Dr. Leo Young (3 copies)  
OUSDRE (R&AT)  
Room 3D1067, The Pentagon  
Washington, D.C. 20301

Dr. Richard L. Garwin  
IBM, T. J. Watson Research Center  
P. O. Box 218  
Yorktown Heights, NY 10598

Dr. Edward T. Gerry, President  
W. J. Schafer Associates, Inc.  
1901 N. Fort Myer Drive  
Arlington, VA 22209

Dr. Avraham Gover  
Tel Aviv University  
Fac. of Engineering  
Tel Aviv, ISRAEL

Mr. Donald L. Haas, Director  
DARPA/STO  
1400 Wilson Boulevard  
Arlington, VA 22209

Dr. P. Hammerling  
La Jolla Institute  
P. O. Box 1434  
La Jolla, CA 92038

Director  
National Security Agency  
Fort Meade, MD 20755  
ATTN: Mr. Thomas Handel, A243

Dr. William Happer  
560 Riverside Drive  
New York City, NY 10027

Dr. Robert J. Hermann  
Assistant Secretary of the  
Air Force (RD&L)  
Room 4E856, The Pentagon  
Washington, D.C. 20330

Dr. Rod Hiddleston  
KMS Fusion  
Ann Arbor, MI 48106

Dr. J. L. Hirshfield (2 copies)  
Yale University  
Mason Laboratory  
400 Temple Street  
New Haven, CT 06520

Dr. R. Hofland  
Aerospace Corp.  
P. O. Box 92957  
Los Angeles, CA 90009

Dr. Fred Hopf  
University of Arizona  
Tucson, AZ 85721

Dr. Benjamin Huberman  
Associate Director, OSTP  
Room 476, Old Executive Office Bldg.  
Washington, D.C. 20506

Dr. S. F. Jacobs  
Optical Sciences Center  
University of Arizona  
Tucson, AZ 85721

Mr. Eugene Kopf  
Principal Deputy Assistant  
Secretary of the Air Force (RD&L)  
Room 4E964, The Pentagon  
Washington, D.C. 20330

Prof. N. M. Kroll  
La Jolla Institute  
P. O. Box 1434  
La Jolla, CA 92038

Dr. Tom Kuper  
Optical Sciences Center  
University of Arizona  
Tucson, AZ 85721

Dr. Thomas Kwan  
Los Alamos National Scientific  
Laboratory  
MS608  
Los Alamos, NM 87545

Dr. Willis Lamb  
Optical Sciences Center  
University of Arizona  
Tucson, AZ 85721

Mr. Mike Lavan  
BMDATC-O  
ATTN: ATC-O  
P. O. Box 1500  
Huntsville, AL 35807

Dr. John D. Lawson (2 copies)  
Rutherford High Energy Lab.  
Chilton  
Didcot, Oxon OX11 0OX  
ENGLAND

Mr. Ray Leadabrand  
SRI International  
333 Ravenswood Avenue  
Menlo Park, CA 94025

Mr. Barry Leven  
NISC/Code 20  
4301 Suitland Road  
Washington, D.C. 20390

Dr. Donald M. LeVine (3 copies)  
SRI International  
1611 N. Kent Street  
Arlington, VA 22209

Dr. Anthony T. Lin  
University of California  
Los Angeles, CA 90024

Director (2 copies)  
National Security Agency  
Fort Meade, MD 20755  
ATTN: Mr. Robert Madden, R/SA

Dr. John Madey  
Physics Department  
Stanford University  
Stanford, CA 94305

Dr. Joseph Mangano  
DARPA  
1400 Wilson Boulevard  
Arlington, VA 22209

Dr. S. A. Mani  
W. J. Schafer Associates, Inc.  
10 Lakeside Office Park  
Wakefield, MA 01880

Dr. Mike Mann  
Hughes Aircraft Co.  
Laser Systems Division  
Culver City, CA 90230

Dr. T. C. Marshall  
Applied Physics Department  
Columbia University  
New York, NY 10027

Mr. John Meson  
DARPA  
1400 Wilson Boulevard  
Arlington, VA 22209

Dr. Pierre Meystre  
Projektgruppe fur Laserforschung  
Max Planck Gesellschaft  
Garching, MUNICH WEST GERMANY

Dr. Gerald T. Moore  
Optical Sciences Center  
University of Arizona  
Tucson, Az 85721

Dr. Philip Morton  
Stanford Linear Accelerator Center  
P. O. Box 4349  
Stanford, CA 94305

Dr. Jesper Munch  
TRW  
One Space Park  
Redondo Beach, CA 90278

Dr. George Neil  
TRW  
One Space Park  
Redondo Beach, CA 90278

Dr. Kelvin Neil  
Lawrence Livermore National Lab.  
Code L-321, P. O. Box 808  
Livermore, CA 94550

Dr. Brian Newnam  
MS 564  
Los Alamos National Scientific  
Laboratory  
P. O. Box 1663  
Los Alamos, NM 87545

Dr. Milton L. Noble (2 copies)  
General Electric Company  
G. E. Electric Park  
Syracuse, NY 13201

Prof. E. Ott (2 copies)  
University of Maryland  
Dept. of Physics  
College Park, MD 20742

Dr. Richard H. Pantell  
Stanford University  
Stanford, CA 94305

Dr. Claudio Parazzoli  
Hughes Aircraft Company  
Building 6, MS/C-129  
Centinela & Teale Streets  
Culver City, CA 90230

Dr. Richard M. Patrick  
AVCO Everett Research Lab., Inc.  
2385 Revere Beach Parkway  
Everett, MA 02149

Dr. Claudio Pellegrini  
Brookhaven National Laboratory  
Associated Universities, Inc.  
Upton, L.I., NY 11973

The Honorable William Perry  
Under Secretary of Defense (R&E)  
Office of the Secretary of Defense  
Room 3E1006, The Pentagon  
Washington, D.C. 20301

Dr. Alan Pike  
DARPA/STO  
1400 Wilson Boulevard  
Arlington, VA 22209

Dr. Hersch Pilloff  
Code 421  
Office of Naval Research  
Arlington, VA 22217

Dr. Charles Planner  
Rutherford High Energy Lab.  
Chilton  
Didcot, Oxon, OX11, OOX  
ENGLAND

Dr. Michal Poole  
Daresbury Nuclear Physics Lab.  
Daresbury, Warrington  
Cheshire WA4 4AD  
ENGLAND

Dr. Don Prosnitz  
Lawrence Livermore National Lab.  
Livermore, CA 94550

Dr. D. A. Reilly  
AVCO Everett Research Lab.  
Everett, MA 02149

Dr. James P. Reilly  
W. J. Schafer Associates, Inc.  
10 Lakeside Office Park  
Wakefield, MA 01880

Dr. A. Renieri  
C.N.E.N.  
Div. Nuove Attivita  
Dentro di Frascati  
Frascati, Rome  
ITALY

Dr. Daniel N. Rogovin  
SAI  
P. O. Box 2351  
La Jolla, CA 92038

Dr. Michael Rosenbluh  
MIT - Magnet Laboratory  
Cambridge, MA 02139

Dr. Marshall N. Rosenbluth  
Institute for Advanced Study  
Princeton, NJ 08540

Dr. Eugene Ruane (2 copies)  
P. O. Box 1925  
Washington, D.C. 20013

Dr. Antonio Sanchez  
MIT/Lincoln Laboratory  
Room 3231  
P. O. Box 73  
Lexington, MA 02173

Dr. Aleksandr N. Sandalov  
Department of Physics  
Moscow University  
MGU, Lenin Hills  
Moscow, 117234, USSR

Prof. S. P. Schlesinger  
Columbia University  
Dept. of Electrical Engineering  
New York, NY 10027

Dr. Howard Schlossberg  
AFOSR  
Bolling AFB  
Washington, D.C. 20332

Dr. Stanley Schneider  
Rotodyne Corporation  
26628 Fond Du Lac Road  
Palos Verdes Peninsula, CA 90274

Dr. Marlan O. Scully  
Optical Science Center  
University of Arizona  
Tucson, AZ 85721

Dr. Steven Segel  
KMS Fusion  
3621 S. State Street  
P. O. Box 1567  
Ann Arbor, MI 48106



Dr. Robert Sepucha  
DARPA/STO  
1400 Wilson Boulevard  
Arlington, VA 22209

Dr. A. M. Sessler  
Lawrence Berkeley Laboratory  
University of California  
1 Cyclotron Road  
Berkeley, CA 94720

Dr. Earl D. Shaw  
Bell Labs  
600 Mountain Avenue  
Murray Hill, NJ 07974

Dr. Chan-Chin Shih  
R&D Associates  
P. O. Box 9695  
Marina Del Rey, CA 92091

Dr. Jack Slater  
Mathematical Sciences, NW  
P. O. Box 1887  
Bellevue, WA 98009

Dr. Kenneth Smith  
Physical Dynamics, Inc.  
P. O. Box 556  
La Jolla, CA 92038

Mr. Todd Smith  
Hansen Labs  
Stanford University  
Stanford, CA 94305

Dr. Joel A. Snow  
Senior Technical Advisor  
Office of Energy Research  
U. S. Department of Energy, M.S. E084  
Washington, D.C. 20585

Dr. Richard Spitzer  
Stanford Linear Accelerator Center  
P. O. Box 4347  
Stanford, CA 94305

Mrs. Alma Spring  
DARPA/Administration  
1400 Wilson Boulevard  
Arlington, VA 22209

DRI/MP Reports Area G037 (2 copies)  
333 Ravenswood Avenue  
Menlo Park, CA 94025  
ATTN: D. Leitner

Dr. Abraham Szoke  
Lawrence Livermore National Lab.  
MS/L-470, P. O. Box 808  
Livermore, CA 94550

Dr. Milan Tekula  
AVCO Everett Research Lab.  
2385 Revere Beach Parkway  
Everett, MA 02149

Dr. John E. Walsh  
Department of Physics  
Dartmouth College  
Hanover, NH 03755

Dr. Wasneski (2 copies)  
Naval Air Systems Command  
Department of the Navy  
Washington, D.C. 20350

Ms. Bettie Wilcox  
Lawrence Livermore National Lab.  
ATTN: Tech. Info. Dept. L-3  
P. O. Box 808  
Livermore, CA 94550

Dr. A. Yariv  
California Institute of Tech.  
Pasadena, CA 91125

FILMED  
5-8